

Quantum Mechanics & Special Relativity

Review

1. Special Relativity

1st Postulate: The laws of physics are the same in all reference frames

2nd Postulate: Nothing can travel faster than 'c'

2. Time Dilation & Length Contraction

Time Dilation: time slows as objects approach the speed of light

$$t = \frac{t_o}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Length Contraction: objects moving at high speeds appear shorter

$$L = L_o \sqrt{1 - \frac{v^2}{c^2}}$$

3. Mass Dilation

Objects moving at speeds approaching the speed of light gain mass

$$m = \frac{m_o}{\sqrt{1 - \frac{v^2}{c^2}}}$$

4. Mass-Energy Equivalence

The momentum and energy of an object are affected by the speed of the object. Objects travelling at speeds approaching the speed of light, experience mass dilation which in turn affects the momentum and energy of the object.

$$p = \frac{m_o v}{\sqrt{1 - \frac{v^2}{c^2}}}; \quad E = m_o c^2 + E_k$$

5. Elementary Particles

Leptons: have no internal structure

Quarks: smallest unit of matter

Hadrons: made up of quarks

Mesons: consist of a quark and antiquark

Baryons: consist of three quarks

Bosons: force carrying particles

6. Quantum Theory

Fundamental problems with wave theory:

- The energy of a system is finite
- Light exhibits the property of momentum
- Particles exhibit the property of diffraction

Light travels in packets of energy called quanta

$$- E_{\gamma} = hf ; E_{\gamma} = \frac{hc}{\lambda}$$

7. The Photoelectric Effect

Energy is transferred from incident photons to the electrons in a metal

$$E_k = E_{\gamma} - W_0 \text{ where } E_k = eV_0$$

If $E_{\gamma} < W_0$ no photoelectrons appear

If $E_{\gamma} = W_0$ the photoelectrons are stopped at the metal surface

If $E_{\gamma} > W_0$ the photoelectrons are ejected

The cut-off potential is the minimum potential required to prevent electrons from being ejected from the metal surface.

8. de Broglie & Matter Waves

Light behaves as both a wave and a particle

$$\lambda = \frac{h}{p} \text{ or } \lambda = \frac{h}{mv}$$

9. Probability Waves

Each particle is represented by a wave function, Ψ (position, time), which represents the probability of finding the particle at that position at that particular instant in time.

10. Heisenberg's Uncertainty Principle

If we know the position of a particle, we cannot know its momentum and vice versa.

$$\Delta p_y \Delta y \geq \hbar$$

If we know the energy of the particle, we cannot know the length of time it has that energy and vice versa.

$$\Delta E \Delta t \geq \hbar$$

11. Questions

- Page 661 #1, 4, 5, 6, 7, 9
- Page 735 #10, 11
- Page 742 #2, 3, 4, 5, 12, 13, 14, 23, 24, 28, 30